665. Molecular Polarisability. A Study of Internal Rotation in the Benzyl Halides and Related Molecules from Measurements of Molar Kerr Constants and Dipole Moments

By R. J. W. Le Fèvre, B. J. Orr, and G. L. D. Ritchie

Molar Kerr constants and apparent dipole moments are recorded for benzyl chloride, benzyl bromide, benzyl iodide, l-chloromethylnaphthalene, 4-chlorobenzyl chloride, 4-bromobenzyl bromide, and benzyl cyanide as solutes in carbon tetrachloride at $25^{\circ}$. The dependence of the molar Kerr constants on molecular conformation is considered, and the results discussed in relation to internal rotation in the molecules. For the first four compounds, the potential-energy function governing internal rotation is estimated from van der Waals interaction data, and average molar Kerr constants calculated therefrom.

This Paper deals with the problem of internal rotation in a number of aromatic molecules containing the $\mathrm{CH}_{2} \mathrm{X}$ substituent group (where $\mathrm{X}=$ halogen or CN ), by the approach recently adopted for 1,2 -dichloroethane. ${ }^{1}$ Molar Kerr constants and dipole moments, measured in carbon tetrachloride at $25^{\circ}$, for seven such compounds are recorded in Tables 1 and 2. The results are then discussed in relation to factors influencing internal rotation of the $\mathrm{CH}_{2} \mathrm{X}$ group in these molecules.
${ }^{1}$ R. J. W. Le Fèvre and B. J. Orr, Austral. J. Chem., 1964, 17, 1098.

Table 1
Incremental Kerr effects, dielectric constants, etc., for solutions in carbon tetrachloride at $25^{\circ}$

| Benzyl chloride |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{5} w_{2} \quad \ldots \ldots \ldots \ldots . .$. | 2039 | 2574 | 4116 | 4539 | 6423 | 6990 |  |
| $10^{4} \Delta \varepsilon$ | 1085 | 1370 | 2187 | 2394 | 3386 | 3702 |  |
| $10^{5} w_{2} \ldots \ldots \ldots \ldots \ldots$. | 2039 | 3458 | 4116 | 5651 | 5683 | 7819 |  |
| $-10^{4} \Delta d \ldots \ldots . . . . .$. | 137 | 237 | 280 | 385 | 381 | 529 |  |
| $10^{5} w_{2} \quad \ldots \ldots \ldots \ldots \ldots .$. | 2924 | 4539 | 4588 | 6990 |  |  |  |
| $10^{4} \Delta n$ | 38 | 57 | 56 | 86 |  |  |  |
| $10^{5} w_{2}$ | 1506 | 1864 | 3196 | 3453 | 5633 | 6534 | 7509 |
| $10^{11} \Delta B$ | 88 | 118 | 175 | 216 | 340 | 401 | 438 |
| $\text { whence } \Sigma \Delta \varepsilon / \Sigma w_{2}=5 \cdot 29 ; \quad \Sigma \Delta d / \Sigma w_{2}=-0.68 ; \Sigma \Delta n / \Sigma w_{2}=0 \cdot 124 ; \Sigma \Delta n^{2} / \Sigma w_{2}=0.36 ;$ |  |  |  |  |  |  |  |
| Benzyl bromide |  |  |  |  |  |  |  |
| $10^{5} w_{2}$ | 1792 | 2752 |  |  | 4628 | 5001 | 6659 |
| $10^{4} \Delta \varepsilon$ | 727 | 1115 |  |  | 1895 | 2047 | 2735 |
| $-10^{5} \Delta d$ | 281 | 359 |  |  | 682 | 703 | 976 |
| $10^{4} \Delta n$ | 25 | 39 |  |  | 64 | 70 | 91 |
| $10^{11} \Delta B$ | 302 | 605 |  |  | 1042 | 1042 | 1364 |

whence $\Sigma \Delta \varepsilon / \Sigma w_{2}=4.08 ; \Sigma \Delta d / \Sigma w_{2}=-0.15 ; \Sigma \Delta n / \Sigma w_{2}=0.139 ; \Sigma \Delta n^{2} / \Sigma w_{2}=0.41 ;$
$\Sigma \Delta B / \Sigma w_{2}=2.13 \times 10^{-7}$
Benzyl iodide

| $10^{5} w_{2}$ | 1126 | 2221 | 3166 | 4080 | 5245 | 6455 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{4} \Delta \varepsilon$ | 309 | 616 | 882 | 1138 | 1466 | 1814 |
| $10^{5} \Delta d$ | 138 | 348 | 474 | 576 | 825 | 964 |
| $10^{4} \Delta n$ | 19 | 38 | 53 | 68 | 89 | 108 |
| $10^{11} \Delta B$ | 486 | 935 | 1276 | 1677 | 2232 | 2841 |

> whence $\Sigma \Delta \varepsilon / \Sigma w_{2}=2.79 ; \quad \Sigma \Delta d / \Sigma w_{2}=0.15 ; \quad \Sigma \Delta n / \Sigma w_{2}=0.168 ; ~ \Sigma \Delta n^{2} / \Sigma w_{2}=0.49 ;$ $\Sigma \Delta B / \Sigma w_{2}=4.24 \times 10^{-7}$

| 1-Chloromethylnaphthalene |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{5} w_{2}$ |  | 1459 | 3025 | 4021 | 4906 |
| $10^{4} \Delta \varepsilon$ |  | 553 | 1378 | 1846 | 2240 |
| $-10^{5} \Delta d$ |  | 789 | 1489 | 2023 | 2446 |
| $10^{4} \Delta n$. |  | 39 | 79 | 111 | 132 |
| $-10^{11} \Delta B$ |  | 465 | 1244 | 1677 | 2189 |

whence $\Sigma \Delta \varepsilon / \Sigma w_{2}=4.49 ; \quad \Sigma \Delta d / \Sigma w_{2}=-0.50 ; \sum_{\Sigma \Delta B / \Sigma w_{2}=-4.16 \times 10^{-7}}^{\Sigma \Delta / \Sigma w_{2}=0.269 ; ~} \Sigma \Delta n^{2} / \Sigma w_{2}=0.79 ;$ $\Sigma \Delta B / \Sigma w_{2}=-4.16 \times 10^{-7}$

4-Chlorobenzyl chloride

| $10^{5} w_{2}$ | 479 | 671 | 921 | 1061 | 1466 | 1903 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{4} \Delta \varepsilon$ | 179 | 254 | 347 | 401 | 555 | 722 |
| $-10^{5} \Delta d$. | 172 | 246 | 321 | 397 | 560 | 725 |
| $10^{4} \Delta n$. | 7 | 10 | 14 | 14 | 23 | 27 |
| $10^{5} w_{2}$ | 479 | 770 | 1061 | 1351 | 1466 | 1903 |
| $-10^{11} \Delta B$ | 228 | 393 | 574 | 702 | 764 | 1002 |

whence $\Sigma \Delta \varepsilon / \Sigma w_{2}=3.78 ; \quad \Sigma \Delta d / \Sigma w_{2}=-0.37 ; \Sigma \Delta n / \Sigma w_{2}=0.146 ; \Sigma \Delta n^{2} / \Sigma w_{2}=0.43 ;$
$\Sigma \Delta B / \Sigma w_{2}=-5.21 \times 10^{-7}$
4-Bromobenzyl bromide

| $10^{5} w_{2}$ | 350 | 837 | 2297 | 2712 | 3016 | 4251 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{4} \Delta \varepsilon$ | 84 | 214 | 590 | 681 | 771 | 1127 |
| $10^{5} \Delta d$ | 97 | 207 | 568 | 661 | 723 | 993 |
| $10^{4} \Delta n$. | 7 | 13 | 38 | 39 | 43 | 65 |
| $-10^{11} \Delta B$ | 139 | 278 | 935 | 1116 | 1239 | 1805 |

whence $\Sigma \Delta \varepsilon / \Sigma w_{2}=2.58 ; \begin{array}{r}\Sigma \Delta d / \Sigma w_{2}=0.24 ; ~ \\ \Sigma \Delta \Delta n / \Sigma w_{2}=0.15 ; ~ \\ \Sigma \Delta w_{2}=-4.09 \times 1 n^{-7} / \Sigma w_{2}=0.46 ;\end{array}$
Benzyl cyanide

| $10^{5} w_{2} \ldots \ldots \ldots \ldots \ldots$. | 212 | 380 | 511 | 723 | 970 | 1109 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $10^{4} \Delta \varepsilon \ldots \ldots \ldots \ldots \ldots$. | 415 | 754 | 1018 | 1434 | 1920 | 2194 |
| $-10^{5} \Delta d \ldots \ldots \ldots \ldots$. | $\mathbf{1 7 1}$ | 312 | 425 | 633 | 808 | 935 |
| $10^{4} \Delta n \ldots \ldots \ldots \ldots \ldots$. | 436 | - | 774 | 1043 | 1438 | 1958 |
| $10^{11} \Delta B \ldots \ldots \ldots \ldots$ | 2196 |  |  |  |  |  |

whence $\Sigma \Delta \varepsilon / \Sigma w_{2}=19.8 ; \Sigma \Delta d / \Sigma w_{2}=-0.84 ; \Sigma \Delta n / \Sigma w_{2}=0.139 ; ~ \Sigma \Delta n^{2} / \Sigma w_{2}=0.41 ;$
$\Sigma \Delta B / \Sigma w_{2}=20.1 \times 10^{-7}$

Table 2
Polarisations, refractions, dipole moments, and molar Kerr constants in carbon tetrachloride

| Solute | $\alpha \varepsilon_{1}$ | $\beta$ | $\gamma^{\prime} n_{1}{ }^{2}$ | $\infty P_{2}$ (c.c.) | $R_{\text {D }}$ (c.c.) | $\mu(\mathrm{D}) *$ | $\gamma$ | $\delta$ | $\begin{gathered} 10^{12} \\ \infty\left({ }_{m} K_{2}\right) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{PhCH}_{2} \mathrm{Cl}$ | $5 \cdot 29$ | $-0.43$ | 0.36 | $104 \cdot 1$ | 36.2 | 1.80 | 0.085 | 8.5 | 6.9 |
| $\mathrm{PhCH}_{2} \mathrm{Br}$ | $4 \cdot 08$ | $-0.09$ | $0 \cdot 41$ | $108 \cdot 3$ | 39.9 | 1.83 | 0.095 | $30 \cdot 4$ | $37 \cdot 8$ |
| $\mathrm{PhCH}_{2} \mathrm{I}$ | $2 \cdot 79$ | 0.09 | $0 \cdot 49$ | $100 \cdot 6$ | $45 \cdot 9$ | 1.60 | 0.115 | $60 \cdot 6$ | 98.1 |
| $1-\mathrm{C}_{10} \mathrm{H}_{7} \mathrm{CH}_{2} \mathrm{Cl} .$. | $4 \cdot 49$ | $-0.32$ | $0 \cdot 79$ | 126.7 | 55.5 | 1.83 | $0 \cdot 185$ | $-59 \cdot 4$ | $-80 \cdot 0$ |
| $4-\mathrm{ClC}_{6} \mathrm{H}_{4} \mathrm{CH}_{2} \mathrm{Cl}$ | $3 \cdot 78$ | $-0.23$ | $0 \cdot 43$ | $100 \cdot 9$ | 41.9 | 1.67 | $0 \cdot 100$ | $-74 \cdot 4$ | -94 |
| $4-\mathrm{BrC}_{6} \mathrm{H}_{4} \mathrm{CH}_{2} \mathrm{Br}$ | 2.58 | $0 \cdot 15$ | $0 \cdot 46$ | $107 \cdot 2$ | $49 \cdot 3$ | $1 \cdot 64$ | $0 \cdot 104$ | $-58 \cdot 4$ | $-110$ |
| PhCH ${ }_{2} \mathrm{CN}$..... | $19 \cdot 8$ | $-0.53$ | 0.41 | $278 \cdot 7$ | $36 \cdot 2$ | $3 \cdot 43$ | 0.095 | 287 | 245 |
| * It is assumed that ${ }_{\mathrm{D}} P=1.05 R_{\mathrm{D}}$. |  |  |  |  |  |  |  |  |  |

## Experimental

Materials.-Liquids were dried and redistilled immediately before use; drying agents and b. p.'s were: for benzyl chloride, sodium sulphate and $179^{\circ} / 760 \mathrm{~mm}$.; for benzyl bromide, sodium sulphate and $130^{\circ} / c a .100 \mathrm{~mm}$.; for 1-chloromethylnaphthalene (prepared as in ref. 2), potassium carbonate and $140^{\circ} / 10 \mathrm{~mm}$.; for benzyl cyanide, sodium sulphate and $118^{\circ} / 25 \mathrm{~mm}$. Benzyl iodide, prepared as in ref. 3, was recrystallised from ethanol at $0^{\circ}$ and had m. p. $24^{\circ}$. 4-Chlorobenzyl chloride, fractionally crystallised, dried over phosphoric oxide, and redistilled at $180^{\circ} / \mathrm{ca} .100 \mathrm{~mm}$., had m. p. $27^{\circ}$. A commercial sample of 4 -bromobenzyl bromide, with m. p. $64^{\circ}$, was used without further purification. Carbon tetrachloride, fractionated and dried over fused calcium chloride, was used throughout as solvent.

Apparatus.-Dielectric constants have been determined with apparatus as in ref. 4, associated procedures giving polarisations being standard. ${ }^{5 a}$ Kerr effects have been recorded photometrically with apparatus as in ref. 6.

Results.-These are listed in usual form in Tables 1 and 2. The symbols used are those previously explained in refs. 4, $5 a$, and $7 a-d$; they have recently been summarised in ref. 8 .

Previous Measurements.-No previous dipole-moment measurements are on record for benzyl iodide, l-chloromethylnaphthalene, or 4-bromobenzyl bromide; the apparent dipole moments of the remaining compounds of the series are in substantial agreement with those recorded in ref. 9. No previous measurements of $\infty\left({ }_{m} K_{2}\right)$ for the compounds listed in Table 2 have been recorded.

## Discussion

Magnitude and Direction of Dipole Moments.-In estimating the directions in which the dipole moments of the molecules of this series act, it has been assumed that the observed moments (Table 2) are the resultants only of primary bond moments, and that the secondary effects of inductive and mesomeric moments may, for the present purposes, be neglected. It has further been assumed that all CCH and CCX bond angles in the $\mathrm{C}_{\mathrm{Ar}}-\mathrm{CH}_{2} \mathrm{X}$ group are $110^{\circ}$. On this basis, the dipole moments of the benzyl halides, 1 -chloromethylnaphthalene, and benzyl cyanide emerge as the resultant of a $\mathrm{C}-\mathrm{X}$ bond moment and three $\mathrm{C}-\mathrm{H}$ bond moments, tetrahedrally disposed. If the dipole moments of the $\mathrm{C}-\mathrm{H}$ bonds in the $\mathrm{CH}_{2} \mathrm{X}$ group and in the 4 -position of the aromatic group are of the same order, the resultant dipole moment, $\mu_{\text {res. }}$, should act along the $\mathrm{C}-\mathrm{X}$ bond axis.

[^0]In the more complicated cases of 4 -chlorobenzyl chloride and 4-bromobenzyl bromide, the dipole moment has been treated as the resultant of the moment, $\mu\left(\mathrm{C}_{\mathrm{Ar}}-\mathrm{X}\right)$, of the para-substituent and of the moment, $\mu\left(\mathrm{CH}_{2} \mathrm{X}\right)$, of the $\mathrm{CH}_{2} \mathrm{X}$ group. The magnitudes of
 $\mu\left(\mathrm{C}_{\mathrm{Ar}}-\mathrm{Cl}\right)$ and $\mu\left(\mathrm{C}_{\mathrm{Ar}}-\mathrm{Br}\right)$ are retained as 1.59 and 1.51 D , respectively, from the appropriate halogenobenzenes; ${ }^{7 b}$ likewise $\mu\left(\mathrm{CH}_{2} \mathrm{Cl}\right)$ and $\mu\left(\mathrm{CH}_{2} \mathrm{Br}\right)$ are adopted as 1.80 and 1.83 D , from the corresponding benzyl halides (Table 2). These data, together with the observed resultant moments, $\mu_{\text {res., }}$ permit the calculation of the directions of $\mu\left(\mathrm{CH}_{2} \mathrm{X}\right)$ and $\mu_{\text {res }}$, defined respectively by angles $\chi$ and $\psi$, as in (I). For 4-chlorobenzyl chloride, $\chi=31 \cdot 5^{\circ}$ and $\psi=23^{\circ}$; for 4-bromobenzyl bromide, $\chi=32^{\circ}$ and $\psi=19^{\circ}$.

Molar Refractions.-Values of $R_{\mathrm{D}}$ (calc.) have been estimated for the molecules of the series by summation of the appropriate bond and group refractions given by Vogel, ${ }^{10}$ no allowance being made for mesomeric or hyperconjugative effects due to the $\mathrm{CH}_{2} \mathrm{X}$ group. The exaltation of refraction, $\Delta R_{\mathrm{D}}$, calculated as the difference between $R_{\mathrm{D}}$ (obs.) and $R_{\mathrm{D}}$ (calc.), gives an estimate of the double-bond character in the $\mathrm{C}_{\mathrm{Ar}}-\mathrm{C}$ bond. Multiplication of $\Delta R_{\mathrm{D}}$ by a factor of ( $9 / 4 \pi \boldsymbol{N}$ ), where $\boldsymbol{N}$ is the Avogadro number, yields the exaltation of polarisability, $\Delta b$, which, in ensuing calculations, has been assumed to be directed along the longitudinal axis of the $\mathrm{C}_{\mathrm{Ar}}-\mathrm{C}$ bond. The results of such calculations are as in Table 3.
Dependence of ${ }_{\mathrm{m}} K$ on Molecular Conformation.-The various possible molecular conformations resulting from internal rotation about the $\mathrm{C}_{\mathrm{Ar}}-\mathrm{C}$ bond may be designated by a parameter $\phi$, which is the angle between the $\mathrm{C}_{\mathrm{Ar}}-\mathrm{C}-\mathrm{X}$ plane and the plane of the aromatic

Table 3
Molar refractions and exaltations of refraction and polarisability *

| Molecule | $\mathrm{PhCH}_{2} \mathrm{Cl}$ | $\mathrm{PhCH}_{2} \mathrm{Br}$ | $\mathrm{PhCH}_{2} \mathrm{I}$ | $1-\mathrm{C}_{10} \mathrm{H}_{7} \mathrm{CH}_{2} \mathrm{Cl}$ | $4-\mathrm{ClC}_{6} \mathrm{H}_{4} \mathrm{CH}_{2} \mathrm{Cl}$ | $4-\mathrm{BrC}_{6} \mathrm{H}_{4} \mathrm{CH}_{2} \mathrm{Br}$ | $\mathrm{PhCH}_{2} \mathrm{CN}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $R_{\text {D }}$ (obs.) | 36.2 | 39.9 | $45 \cdot 9$ | 55.5 | 41.9 | $49 \cdot 3$ | 36.2 |
| $R_{\text {D }}$ (calc.) | $35 \cdot 7$ | $38 \cdot 6$ | $43 \cdot 8$ | $54 \cdot 2$ | 41.4 | 47-1 | $35 \cdot 3$ |
| $\Delta R_{\text {D }}$ | $+0.5$ | +1.3 | +2.2 | $+1.4$ | $+0.5$ | +2.2 | $+0.9$ |
| $\Delta b$ | $0 \cdot 59$ | 1.55 | $2 \cdot 62$ | $1 \cdot 66$ | $0 \cdot 59$ | 2.62 | 1.07 |

* Refractions are expressed in c.c. units; polarisabilities, here and elsewhere, are in cubic Ångström units ( $\mathbf{1 0} 0^{-24}$ c.c.).
ring. For 1-chloromethylnaphthalene, we take $\phi=0^{\circ}$ when the chlorine atom is cisoriented with respect to the 8 -position of the $\alpha$-naphthyl group, and $\phi=180^{\circ}$ when it is trans-oriented. For a number of values of $\phi$, molecular polarisability semi-axes, $b_{1}, b_{2}, b_{3}$, have been estimated by addition of bond- and group-polarisability tensors and diagonalisation of the resulting matrices, following standard procedures. ${ }^{5 b, 11}$ The bond- and group-polarisability semi-axes, $b_{\mathrm{L}}, b_{\mathrm{T}}, b_{\mathrm{V}}$, used are given in Table 4. The $b_{\mathrm{L}}$ of the $\mathrm{C}_{\mathrm{Ar}}-\mathrm{C}$ bond has been calculated as the sum of the usual $b_{\mathrm{L}}$ of the $\mathrm{C}-\mathrm{C}$ bond and the $\Delta b$ as in Table 3 . Calculations have been performed with two sets of $\mathrm{C}-\mathrm{X}$ bond-polarisabilities, obtained (i) from $\mathrm{CH}_{3} \mathrm{X}$, and (ii) from $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CX}$. The resultant molecular polarisabilities, in conjunction with the dipole-moment components, $\mu_{1}, \mu_{2}, \mu_{3}$, along the axes of $b_{1}, b_{2}, b_{3}$, respectively, yield values of ${ }_{\mathrm{m}} K$ (calc.) as in Table 5 .

The values of ${ }_{\mathrm{m}} K$ (calc.) for all the compounds have been found to satisfy closely a function of the form

$$
\begin{equation*}
10^{12}{ }_{\mathrm{m}} K(\phi)=a+b \cos 2 \phi \tag{1}
\end{equation*}
$$

The parameters $a$ and $b$, constants for a given molecule and choice of $\mathrm{C}-\mathrm{X}$ bond polarisabilities, are listed, together with observed molar Kerr constants, ${ }_{\mathrm{m}} K$ (obs.), in Table 6.
${ }_{10}$ A. I. Vogel, $J ., 1948,654$; A. I. Vogel, W. T. Cresswell, G. H. Jeffery, and J. Leicester, J., 1952, 514.
${ }^{\text {in }}$ J. M. Eckert and R. J. W. Le Fèvre, J., 1962, 1081.

Table 4
Assumed bond and group polarisability values

| Bond or group | $b_{\text {L }}$ | $b_{\text {T }}$ | $b_{\text {v }}$ | Bond or group environment | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| C-H .................. | $0 \cdot 64$ | $0 \cdot 64$ | $0 \cdot 64$ | Paraffins | $5 b$ |
| $\mathrm{C}-\mathrm{C}$ | 0.99 | 0.27 | $0 \cdot 27$ | Cyclohexane | $5 b$ |
| $\mathrm{C}-\mathrm{Cl}$ | $3 \cdot 2$ | $2 \cdot 2$ | $2 \cdot 2$ | $\mathrm{CH}_{3} \mathrm{Cl}$ | $5 b$ |
| $\mathrm{C}-\mathrm{Cl}$ | $4 \cdot 0$ | $1 \cdot 6$ | $1 \cdot 6$ | $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CCl}$ | $5 b$ |
| $\mathrm{C}-\mathrm{Br}$ | $4 \cdot 65$ | $3 \cdot 1$ | 3-1 | $\mathrm{CH}_{3} \mathrm{Br}$ | $5 b$ |
| $\mathrm{C}-\mathrm{Br}$ | $6 \cdot 0$ | $2 \cdot 6$ | $2 \cdot 6$ | $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CBr}$ | $5 b$ |
| $\mathrm{C}-\mathrm{I}$ | $6 \cdot 8$ | $4 \cdot 7$ | $4 \cdot 7$ | $\mathrm{CH}_{3} \mathrm{I}$ | $5 b$ |
| C-I | $9 \cdot 2$ | 3.7 | $3 \cdot 7$ | $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CI}$ | $12 a$ |
| $\mathrm{C}-\mathrm{CN}$ | $3 \cdot 64$ | 1.75 | 1.75 | $\mathrm{CH}_{3} \mathrm{CN}$ | $12 b$ |
| $\mathrm{C}-\mathrm{CN}$ | $4 \cdot 03$ | 1.54 | 1.54 | $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CCN}$ | $12 b$ |
| $\mathrm{C}_{6} \mathrm{H}_{5}$ | 10.56 | 10.56 | 6.72 | $\mathrm{C}_{6} \mathrm{H}_{6}$ | 13 |
| $\alpha-\mathrm{C}_{10} \mathrm{H}_{7}$ | $20 \cdot 86$ | 16.96 | $9 \cdot 66$ | $\mathrm{C}_{10} \mathrm{H}_{8}$ | $7 e$ |
| $4-\mathrm{ClC}_{6} \mathrm{H}_{4}$ | 14.08 | 11.80 | $7 \cdot 54$ | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Cl}$ | $7 b$ |
| $4-\mathrm{BrC}_{6} \mathrm{H}_{4}$ | 16.20 | 11.49 | 8.92 | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Br}$ | $7 b$ |

Table 5
Values of $10^{12}{ }_{\mathrm{m}} K$ (calc.) for various conformations

| (i) $b^{\text {cx }}$ as in $\mathrm{CH}_{3} \mathrm{X}$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 0 | 30 | 60 | 90 |
| $+102.2$ | +55.6 | $-38 \cdot 1$ | $-84 \cdot 6$ |
| $+119 \cdot 0$ | $+70 \cdot 0$ | -28.1 | $-77 \cdot 2$ |
| +106.3 | $+67 \cdot 6$ | $-9.8$ | $-48.2$ |
| +324.5 | +183.8 | -98.1 | -239.3 |
| +69.6 | $+26.7$ | $-59.8$ | -102.5 |
| +20.7 | -6.2 | $-60 \cdot 3$ | $-87.3$ |
| $+434 \cdot 6$ | +267.1 | $-68.0$ | $-236.0$ |


| (ii) $b^{\mathrm{cX}}$ as in $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CX}$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 0 | 30 | 60 | 90 |
| $+156.5$ | $+108.2$ | $+11.0$ | $-37.7$ |
| +193.5 | +142.1 | $+39 \cdot 6$ | $-11.9$ |
| +2178 | $+175.1$ | $+89.1$ | +46.2 |
| +387.2 | $+241.0$ | $-51.4$ | -197.4 |
| +86.5 | +41.7 | -49.1 | $-93.9$ |
| +44.7 | +16.2 | $-41 \cdot 1$ | $-69.5$ |
| +516.2 | +348.3 | +11.3 | - 156.5 |

Table 6
Coefficients of the function, ${ }_{\mathrm{m}} K(\phi)=a+b \cos 2 \phi$

| Molecule |  | (i) $b^{\mathrm{Cx}}$ as in $\mathrm{CH}_{3} \mathrm{X}$ |  | (ii) $b^{\mathrm{ox}}$ as in $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CX}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $10^{12}{ }_{\mathrm{m}} K$ (obs.) | $a$ | $b$ | $a$ | $b$ |
| $\mathrm{PhCH}_{2} \mathrm{Cl}$ | +6.9 | 8.7 | $93 \cdot 4$ | 59.5 | $97 \cdot 1$ |
| $\mathrm{PhCH}_{2} \mathrm{Br}$ | $+37.8$ | $20 \cdot 9$ | $98 \cdot 1$ | $90 \cdot 8$ | $102 \cdot 5$ |
| $\mathrm{PhCH}_{2} \mathrm{I}$ | +98.1 | $29 \cdot 0$ | $77 \cdot 2$ | $132 \cdot 1$ | $85 \cdot 8$ |
| 1- $\mathrm{C}_{10} \mathrm{H}_{3} \cdot \mathrm{CH}_{2} \mathrm{Cl}$ | $-80.0$ | $42 \cdot 7$ | 281.9 | $94 \cdot 8$ | 292.2 |
| 4 - $\mathrm{ClC}_{6} \mathrm{H}_{4} \cdot \mathrm{CH}_{2} \mathrm{Cl}$ | -94 | $-16 \cdot 4$ | 86.0 | -3.8 | $90 \cdot 2$ |
| $4-\mathrm{BrC}_{6} \mathrm{H}_{4} \cdot \mathrm{CH}_{2} \mathrm{Br}$ | -110 | $-33 \cdot 3$ | $54 \cdot 0$ | $-12.4$ | $57 \cdot 1$ |
| $\mathrm{PhCH}_{2} \cdot \mathrm{CN} \ldots \ldots$. | $+245$ | $99 \cdot 3$ | $335 \cdot 3$ | $179 \cdot 8$ | 336.4 |

Comparison of ${ }_{\mathrm{m}} \mathrm{K}$ (obs.) and ${ }_{\mathrm{m}} \mathrm{K}$ (calc.). -The values of ${ }_{\mathrm{m}} K$ (calc.) are most simply compared with those of ${ }_{m} K$ (obs.) by evaluation of the quantity $\langle\phi\rangle$; namely the $\phi$, which for each set of conformations, satisfies the relation ${ }_{\mathrm{m}} K(\phi)={ }_{\mathrm{m}} K$ (obs.). Such a parameter has been successfully employed in interpreting Kerr-effect results on numerous previous occasions (see, for example, refs. 14 and 15). Only in cases where molecular rigidity is to be expected, however, will $\langle\phi\rangle$ designate the actual molecular conformation; for more flexible molecules, nevertheless, values of $\langle\phi\rangle$ are sometimes useful in indicating trends in conformational distribution within a series.

Table 7 lists values of $\langle\phi\rangle$, estimated from the data of Table 6 , for the members of the present series. Inspection of Table 7 reveals that expected trends in mean or effective conformation can in no way be associated with the trends in $\langle\phi\rangle$. Thus, for the three benzyl halides, $\langle\phi\rangle$ decreases with increasing molecular weight; this is contrary to expectations based on simple steric requirements. Likewise, the two 4 -halogeno-compounds
${ }_{13}$ R. J. W. Le Fèvre, B. J. Orr, and G. L. D. Ritchie, (a) unpublished data; (b) J., 1965, 2499.
${ }_{13}^{13}$ M. J. Aroney and R. J. W. Le Fèvre, J., 1960, 3600.
${ }_{14}$ M. J. Aroney, R. J. W. Le Fèvre, and J. D. Saxby, J., 1963, 1739; Canad. J. Chem., 1964, 42, 1493.
${ }^{15}$ M. J. Aroney, M. G. Corfield, and R. J. W. Le Fèvre, J., 1964, 648.

Table 7

| Values of $\langle\phi\rangle$ (in degrees) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Molecule | $\mathrm{PhCH}_{2} \mathrm{Cl}$ | $\mathrm{PhCH}_{2} \mathrm{Br}$ | $\mathrm{PhCH}_{2} \mathrm{I}$ | 1-C ${ }_{10} \mathrm{H}_{7} \cdot \mathrm{CH}_{2} \mathrm{Cl}$ |
| (i) $b^{\text {ox }}$ as in $\mathrm{CH}_{3} \mathrm{X}$. $\ldots \ldots \ldots \ldots$. | 46 | 40 | 13 | 58 |
| (ii) $b^{\text {CX }}$ as in $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CX} \quad \ldots \ldots \ldots$ | 62 | 60 | 56 | 64 |
| Molecule | $4-\mathrm{ClC}_{6} \mathrm{H}_{4} \cdot \mathrm{CH}_{2} \mathrm{Cl}$ | $4-\mathrm{Br}$ | $\mathrm{CH}_{2} \mathrm{Br}$ | $\mathrm{PhCH}_{2} \cdot \mathrm{CN}$ |
| (i) $b^{\text {ax }}$ as in $\mathrm{CH}_{3} \mathrm{X} \quad \ldots \ldots \ldots \ldots$. | 77 |  |  | 32 |
| (ii) $b^{\mathrm{OX}}$ as in $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CX} \ldots \ldots \ldots \ldots$. | 90 |  |  | 36 |

* For 4 -bromobenzyl bromide, ${ }_{\mathrm{m}} K$ (obs.) is outside the range of values of ${ }_{\mathrm{m}} K$ (calc.)
yield results which deviate considerably from those for the remainder of the series. Furthermore, benzyl cyanide has an unexpectedly low value of $\langle\phi\rangle$. It can only be concluded, therefore, that evaluation of $\langle\phi\rangle$ is inadequate as a means of studying factors influencing internal rotation in the benzyl halide series.

A more realistic approach to the problem of internal rotation in this series involves the potential-energy function, $U(\phi)$, which determines the distribution amongst the various possible molecular conformations. The value $\left\langle_{\mathrm{m}} K\right\rangle$, of the molar Kerr constant averaged over all conformations is given ${ }^{\mathbf{1}}$ by:

$$
\begin{equation*}
\left\langle_{\mathrm{m}} K\right\rangle=\int_{-\pi}^{\pi} K(\phi) \exp [-U(\phi) / \boldsymbol{k} T] \mathrm{d} \phi \int_{-\pi}^{\pi} \exp [-U(\phi) / \boldsymbol{k} T] \mathrm{d} \phi, \tag{2}
\end{equation*}
$$

where $\boldsymbol{k}$ and $T$ are the Boltzmann constant and absolute temperature, respectively. It is possible to define an equivalent potential function of the form:

$$
\begin{equation*}
U(\phi)=v_{0}(1+\cos 2 \phi) / 2 \tag{3}
\end{equation*}
$$

where $v_{0}$ is the equivalent potential-energy barrier restricting internal rotation at $\phi=0^{\circ}$, and is chosen such that $\left\langle{ }_{\mathrm{m}} K\right\rangle={ }_{\mathrm{m}} K$ (obs.). The parameter $v_{0}$ is not to be identified [except when $U(\phi)$ is in fact of sinusoidal form] with the actual potential barrier at $\phi=0^{\circ}$; it might nevertheless be expected, in certain series of compounds, to indicate trends in their steric hindrance. Such a treatment can generally be successful, however, only if the sinusoidal function of equation (3) is a reasonably good approximation to the actual $U(\phi)$ of each member of the series.

Combination of equations $1-3$ leads to the relation:

$$
\begin{equation*}
10^{12}\left\langle_{\mathrm{m}} K\right\rangle=a+b L\left(v_{0} / 2 \boldsymbol{k} T\right), \tag{4}
\end{equation*}
$$

where $L\left(v_{0} / 2 \boldsymbol{k} T\right)$ is the Langevin function in $v_{0} / 2 \boldsymbol{k} T$. Putting $\left\langle{ }_{\mathrm{m}} K\right\rangle={ }_{\mathrm{m}} K$ (obs.), and with the data of Table 6 , values of $v_{0}$ emerge as in Table 8.

Table 8
Values of equivalent potential-energy barrier, $v_{0}$ (in kcal./mole)


* For 4-bromobenzyl bromide, ${ }_{\mathrm{m}} K$ (obs.) is outside the range of values of ${ }_{\mathrm{m}} K$ (calc.).

The values and trends of the parameter, $v_{0}$, of Table 8 are seen to be just as much in conflict with expectations as are the $\langle\phi\rangle$ values of Table 7. It must therefore be concluded that this approach, too, is inadequate as a means of studying internal rotation in these molecules. Consequently, such semi-empirical approaches as those involving $\langle\phi\rangle$ and $v_{0}$ have been abandoned, and theoretical calculations made of the actual potential function, $U(\phi)$. No further calculations have been performed for the two 4-halogeno-compounds
owing to the apparently anomalous results of Tables 7 and 8, or for benzyl cyanide, for which insufficient data are available to permit calculation of $U(\phi)$.

Estimation of $U(\phi)$ and $\left\langle_{\mathrm{m}} K\right\rangle$.-For the benzyl halides and 1-chloromethylnaphthalene, an attempt has been made to obtain a better estimate of $U(\phi)$ than is provided by the equivalent potential function of equation (3). A consideration of molecular models suggests that it is reasonable to assume that van der Waals forces of attraction and repulsion predominate in determining $U(\phi)$ for these molecules, and that other effects (such as deformations of bond angles, torsional hindrances, dipole-dipole interactions, and solutesolvent interactions) may, for the present purposes, be neglected. Estimates of $U(\phi)$ have therefore been obtained from potential-energy functions for van der Waals interactions of a number of non-bonded pairs of atoms, by the methods in ref. 16. The functions are of the form:

$$
\begin{equation*}
U / \varepsilon=-2.25 \alpha^{-6}+8.28 \times 10^{5} \exp (-\alpha / 0.0736) \tag{5}
\end{equation*}
$$

where $U$ is the potential energy for van der Waals interactions between two non-bonded atoms whose nuclei are separated by a distance $\alpha$ (expressed in units of the sum of their van der Waals radii), and $\varepsilon$ is a constant which depends on the pair of atoms involved. Values of the constant $\varepsilon$ for the interaction of hydrogen (bonded to carbon) with a number of atoms Y (bonded to carbon), ${ }^{16}$ and of the van der Waals radius, $R_{\mathrm{Y}}$ for the atom $\mathrm{Y}^{17}$ are listed in Table 9.

Table 9
Data for non-bonded interactions of H (to C ) with Y (to C) ${ }^{14,15}$

| Atom Y | H | Cl | Br | I |
| :---: | :---: | :---: | :---: | :---: |
| $R_{\mathrm{Y}}(\AA) \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$ | $1 \cdot 20$ | $\mathbf{1 . 8 0}$ | $\mathbf{1 . 9 5}$ | $\mathbf{2 . 1 5}$ |
| $\varepsilon($ kcal./mole $) \ldots \ldots \ldots \ldots \ldots \ldots$. | 0.042 | 0.115 | 0.136 | 0.158 |

Table 10
Estimates of $U(\phi)$ (in kcal./mole) from van der Waals interactions

| Benzyl chloride |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\phi$........ | 0 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 |
| $U(\phi) \ldots \ldots$ | 1.36 | $1 \cdot 18$ | $0 \cdot 80$ | $0 \cdot 42$ | $0 \cdot 16$ | 0.04 | 0.01 | 0.00 | 0.00 | 0.01 |
| Benzyl bromide |  |  |  |  |  |  |  |  |  |  |
|  | 0 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 |
| $U(\phi) \ldots \ldots$ | 2.55 | $2 \cdot 25$ | 1.52 | $0 \cdot 81$ | $0 \cdot 33$ | $0 \cdot 10$ | 0.02 | $0 \cdot 00$ | $0 \cdot 00$ | $0 \cdot 00$ |
| Benzyl iodide |  |  |  |  |  |  |  |  |  |  |
| $\phi$........ | 0 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 |
| $U(\phi) \ldots \ldots$ | $4 \cdot 86$ | $4 \cdot 28$ | 2.94 | $1 \cdot 61$ | $0 \cdot 70$ | 0.23 | 0.06 | 0.01 | $0 \cdot 00$ | $0 \cdot 00$ |
| 1-Chloromethylnaphthalene |  |  |  |  |  |  |  |  |  |  |
| $\phi$........ | 0 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 |
| $U(\phi) \ldots .$. | 236.6 | 191.4 | 105•7 | $43 \cdot 8$ | 14.6 | 4.02 | 0.79 | 0.01 | 0.06 | 0.58 |
|  | 100 | 110 | 120 | 130 | 140 | 150 | 160 | 170 | 180 |  |
| $U(\phi) \ldots .$. | $1 \cdot 48$ | $2 \cdot 45$ | $2 \cdot 88$ | 2.50 | 1.65 | 1.01 | $0 \cdot 85$ | 0.96 | 1.07 |  |

For the benzyl halides, the values of $U(\phi)$ have been estimated for a number of values of $\phi$ as the sum of the separate interaction energies, $U$, for the atom X and the two protons of the $\mathrm{CH}_{2} \mathrm{X}$ group with both ortho protons of the phenyl group. This involves calculating the variation with $\phi$ of a number of interatomic distances and substituting, together with the data of Table 9, into equation (5). Average bond lengths ${ }^{18}$ (in $\AA$ ) assumed are: $\mathrm{C}-\mathrm{H}=1.101 ; \quad \mathrm{C}-\mathrm{Cl}=1.767 ; \quad \mathrm{C}-\mathrm{Br}=1.937 ; \quad \mathrm{C}-\mathrm{I}=2.135 ; \quad \mathrm{C}-\mathrm{C}=1.541 ; \quad \mathrm{C}_{\mathrm{Ar}}-\mathrm{C}_{\mathrm{Ar}}=$ 1.395 . A similar treatment for 1-chloromethylnaphthalene yields the interaction energies

[^1]of the chloromethyl group with the 2 - and 8 -protons of the naphthyl group. Values of the functions $U(\phi)$, adjusted such that their minimum values are zero, are as in Table 10.

Values of $\left\langle_{\mathrm{m}} K\right\rangle$, estimated by substituting the results of Tables 6 and 10 into equation (2), are as in Table 11. The results have been calculated by evaluating, plotting, and graphically integrating the functions $\exp [-U(\phi) / \boldsymbol{k} T]$ and ${ }_{\mathrm{m}} K(\phi) \exp [-U(\phi) / \boldsymbol{k} T]$ between $\phi=0^{\circ}$ and $\phi=180^{\circ}$.

Table 11
Values of $\left\langle_{\mathrm{m}} K\right\rangle$ calculated from $U(\phi)$

| Molecule | $\mathrm{PhCH}_{2} \mathrm{Cl}$ | $\mathrm{PhCH}_{2} \mathrm{Br}$ | $\mathrm{PhCH}_{2} \mathrm{I}$ | $1-\mathrm{C}_{10} \mathrm{H}_{7} \cdot \mathrm{CH}_{2} \mathrm{Cl}$ |
| :---: | :---: | :---: | :---: | :---: |
| $10^{12}$, $K$ ( ${ }^{\text {(i) }} b^{\text {cx }}$ as in $\mathrm{CH}_{3} \mathrm{X}$ | -23.2 | $-26.2$ | $-18.3$ | $-94 \cdot 7$ |
| $10^{12}\left\langle{ }_{m} K\right\rangle\left\{\left(\right.\right.$ ii) $b^{\mathrm{cX}}$ as in $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CX}$ | $+26.0$ | +41.5 | $+80 \cdot 3$ | $-48.1$ |
| $10^{12}{ }_{\mathrm{m}} \mathrm{K}$ (obs.) | $+6.9$ | $+37.8$ | +98.1 | -80.0 |

Table 11 shows that the values of ${ }_{m} K$ (obs.) for the four molecules are generally within the range of calculated values of $\left\langle_{\mathrm{m}} K\right\rangle$ indicating that the experimental results are reasonably consistent with the figures for $U(\phi)$ in Table 10. Although trends in the appropriateness of $b^{0 X}$ are apparent, the nature of the approximations and assumptions inherent in the treatment do not justify any definite conclusions as to choice of bond polarisabilities, and direction of $\mu_{\text {res }}$, or the previously neglected effects of bond-angle deformation, torsional hindrance, dipole-dipole interactions, and solute-solvent interactions.

The award (to B. J. O.) of a C.S.I.R.O. Senior Postgraduate Studentship, allowing completion of part of this work, is gratefully acknowledged.


[^0]:    ${ }^{2}$ A. I. Vogel, " Practical Organic Chemistry," Longmans, London, 3rd edn., 1959, p. 540.
    ${ }^{3}$ G. H. Coleman and C. R. Hauser, J. Amer. Chem. Soc., 1928, 50, 1196 ; 1929, 51, 1497.
    ${ }^{4}$ A. D. Buckingham, J. Y. H. Chau, H. C. Freeman, R. J. W. Le Fèvre, D. A. A. S. Narayana Rao, and J. Tardif, $J ., 1956,1405$.
    ${ }^{5}$ R. J. W. Le Fèvre, (a) " Dipole Moments," Methuen, London, 3rd edn., 1953, ch. 2; (b) J. Proc. Roy. Soc. New South Wales, 1961, 95, 1.
    ${ }^{6}$ R. J. W. Le Fèvre and G. L. D. Ritchie, J., 1963, 4933.
    ${ }^{7}$ C. G. Le Fèvre and R. J. W. Le Fèvre, (a) J., 1953, 4041; (b) J., 1954, 1577; (c) Rev. Pure Appl. Chem. (Australia), 1955, 5, 261; (d) in " Physical Methods of Organic Chemistry," ed. A. Weissberger, Interscience Publ. Inc., New York, 3rd edn., vol. I, p. 2459; (e) J., 1955, 1641.
    ${ }^{8}$ R. J. W. Le Fèvre and K. M. S. Sundaram, $J$., 1962, 1494.
    ${ }^{9}$ L. G. Wesson, "Tables of Electric Dipole Moments," Technology Press, M.I.T., 1948; A. L. McClellan, " Tables of Experimental Dipole Moments," Freeman and Co., San Francisco, 1963.

[^1]:    ${ }^{16}$ T. L. Hill, J. Chem. Phys., 1948, 16, 399; N. L. Allinger, J. Allinger, L. A. Freiberg, R. F. Czaja, and N. A. Le Bel, $J$. Amer. Chem. Soc., 1960, 82, 5882.
    ${ }^{17}$ L. Pauling, "The Nature of the Chemical Bond," Cornell University Press, Ithaca, 2nd edn., 1940, p. 189.
    ${ }^{18}$ L. E. Sutton et al., "Tables of Interatomic Distances and Configuration in Molecules and Ions," Chem. Soc. Special Publ., No. 11, 1958.

